

Fórmulas trigonométricas

$$\begin{array}{lll}
 \sec x = \frac{1}{\cos x}, \csc x = \frac{1}{\sin x} & \sin \frac{\pi}{6} = \frac{1}{2}, \sin \frac{\pi}{3} = \frac{\sqrt{2}}{2} & \arccos 0 = \frac{\pi}{2} \\
 \sin 2x = 2 \sin x \cos x & \sin 0 = 0, \cos 0 = 1, \tan 0 = 0 & \arccos 1 = 0 \\
 \cos 2x = 1 - 2 \sin^2 x & \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}, \tan \frac{\pi}{6} = \frac{\sqrt{3}}{3} & \arctan(\pm\infty) = \pm \frac{\pi}{2} \\
 \cos 2x = 2 \cos^2 x - 1 & \sin \frac{\pi}{6} = \frac{\sqrt{3}}{2}, \sin \frac{\pi}{2} = 1 & \arctan(-1) = -\frac{\pi}{4} \\
 1 + \tan^2 x = \frac{1}{\cos^2 x} & \cos \frac{\pi}{3} = \frac{1}{2}, \tan \frac{\pi}{3} = \sqrt{3} & \arctan 0 = 0 \\
 1 + \cot^2 x = \frac{1}{\sin^2 x} & \cos \frac{\pi}{2} = 0, \tan \frac{\pi}{2} = \infty & \arcsin(-1) = \frac{3\pi}{2} \\
 \sin^2 x + \cos^2 x = 1 & \arcsin 0 = 0, & \arctan 1 = \frac{\pi}{4} \\
 \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}, \tan \frac{\pi}{4} = 1 & \arccos(-1) = \pi; & \arcsin 1 = \frac{\pi}{2} \\
 \sin(\arcsin x) = \cos(\arccos x) = x & \tan(\arctan x) = \cot(\operatorname{arccot} x) = x & \\
 \sin(\arccos x) = \cos(\arcsin x) = \sqrt{1-x^2} & \tan(\arcsin x) = \cot(\arccos x) = \frac{x}{\sqrt{1-x^2}} & \\
 \sin(\arctan x) = \cos(\operatorname{arccot} x) = \frac{x}{\sqrt{1+x^2}} & \tan(\arccos x) = \cot(\arcsin x) = \frac{\sqrt{1-x^2}}{x} & \\
 \sin(\operatorname{arccot} x) = \cos(\arctan x) = \frac{1}{\sqrt{1+x^2}} & \tan(\operatorname{arccot} x) = \cot(\arctan x) = \frac{1}{x} &
 \end{array}$$

Outras Fórmulas

$$\begin{array}{lll}
 \ln A + \ln B = \ln AB & \ln A - \ln B = \ln \frac{A}{B} & A \ln B = \ln B^A \\
 \ln 1 = 0, \ln(+\infty) = +\infty & \ln e = 1, e^0 = 1 & \ln 0^+ = -\infty \\
 e^{-\infty} = 0, e^{+\infty} = +\infty & e^A e^B = e^{A+B} & \frac{e^A}{e^B} = e^{A-B} \\
 (a \pm b)^2 = a^2 \pm 2ab + b^2 & \sqrt{A+B} \neq \sqrt{A} + \sqrt{B} & \sqrt{A^n} = (\sqrt{A})^n \\
 (a^2 - b^2) = (a-b)(a+b) & \sqrt{AB} = \sqrt{A}\sqrt{B} & \sqrt{A/B} = \frac{\sqrt{A}}{\sqrt{B}} \\
 (a^3 - b^3) = (a-b)(a^2 + ab + b^2) & \frac{A+B}{C} = \frac{A}{C} + \frac{B}{C} & (\sqrt{A})^3 = A\sqrt{A} \\
 (a^3 + b^3) = (a+b)(a^2 - ab + b^2) & \frac{A}{B+C} \neq \frac{A}{B} + \frac{A}{C} & \sqrt[m]{A^n} = A^{n/m}
 \end{array}$$

Algumas regras de derivação

$$\begin{array}{lll}
 (u^n)' = nu^{n-1}u' & (e^u)' = u'e^u & (\log u)' = \frac{u'}{u} \\
 (\sin u)' = u' \cos u & (\cos u)' = -u' \sin u & (\tan u)' = \frac{u'}{\cos^2 u} \\
 (\arcsin u)' = \frac{u'}{\sqrt{1-u^2}} & (\arctan u)' = \frac{u'}{1+u^2} & (\cot u)' = -\frac{u'}{\sin^2 u} \\
 (ku)' = ku' & (uv)' = u'v + uv' & \left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}
 \end{array}$$

Regras de primitivação

$$Pk u = kPu$$

$$P1 = x$$

$$Pu^n u' = \frac{u^{n+1}}{n+1} + c$$

$$Pe^x = e^x$$

$$Pe^u u' = e^u + c$$

$$P \sin x = -\cos x$$

$$Pu' \sin u = -\cos u + c$$

$$P \frac{u'}{\sin^2 u} = -\cot u + c$$

$$P \frac{1}{\sqrt{1-x^2}} = \arcsin x = -\arccos x + c$$

$$P \frac{u'}{\sqrt{a^2-u^2}} = \arcsin \frac{u}{a} = -\arccos \frac{u}{a} + c$$

$$P \frac{u'}{1+u^2} = \arctan u + c$$

$$Pu' \sec u = \log |\sec u + \tan u| + c$$

$$Px^n = \frac{x^{n+1}}{n+1} + c$$

$$P \frac{1}{x} = \ln |x|$$

$$P \frac{u'}{u} = \log |u| + c$$

$$Pa^u u' = \frac{a^u}{\log a} + c$$

$$P \cos x = \sin x$$

$$Pu' \cos u = \sin u + c$$

$$P \frac{u'}{\cos^2 u} = \tan u + c$$

$$P \frac{u'}{\sqrt{1-u^2}} = \arcsin u = -\arccos u + c$$

$$P \frac{1}{1+x^2} = \arctan x + c$$

$$P \frac{u'}{a^2+u^2} = \frac{1}{a} \arctan \frac{u}{a} + c$$

$$Pu' \csc u = \log |\csc u - \cot u| + c$$

Primitivação por Partes: $\boxed{Pu'v = uv - Puv'}$

Primitivação por Substituição

Função com	$x = g(t)$	$g'(t)$	$t = g^{-1}(x)$
$\sqrt{a^2 - x^2}$	$x = a \sin t$	$x' = a \cos t$	$t = \arcsin \frac{x}{a}$
$\sqrt{a^2 + x^2}$	$x = a \tan t$	$x' = a \sec^2 t$	$t = \arctan \frac{x}{a}$
$\sqrt{x^2 - a^2}$	$x = a \sec t$	$x' = a \sec t \tan t$	$t = \operatorname{arcsec} \frac{x}{a}$
e^{kx}	$\ln t$	$\frac{1}{t}$	e^x
$\ln^k x$	e^t	e^t	$\ln x$